

1- Similar to the proof of Taylor expansion, find the first 3 terms of  $f(x) = e^x$  around zero. Hint: start with  $\int_0^x e^x dx = e^x - e^0$

2- Use expansion of  $e^x = \sum_1^{\infty} \frac{x^n}{n!}$  to explain the expansions for  $\sin x$ ,  $\cos x$ . Clearly explain the sign changes in the alternative terms.

3- Prove that hyper-harmonic series  $\sum_1 \frac{1}{n^p}$  converges if  $p > 1$

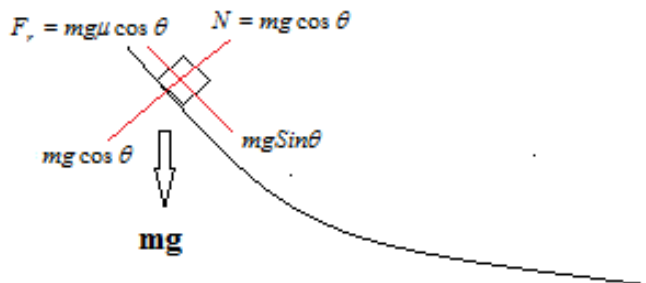
4- Show that  $\sum_0^n \frac{(-1)^n}{2n+1}$  converges conditionally and then find the value of the sum

5- Show that  $\sum_0^n \frac{(-1)^n n}{2^n (2n+1)}$  converges absolutely and then find the value of the sum

6- Solve the DE  $\frac{dy}{dx} - 2y = -2$  at point  $(0,3)$  by series solution. Find the compact form of the solution and then find the function that satisfies the solution.

7- What is (are) the point(s) on any differentiable function (Curve) that the curvature is maximum? Show it mathematically

8- A box (weight = 10N) is sliding down on a track ( $y = 1/x$ ) from  $x = 1$  to  $x = 2$ . If the track coefficient of friction is  $\mu_k = 0.1$ , what is the value of frictional force at  $x = 2$ ? Hint: consider the curvature of the curve at  $x = 2$



9- From the definition of Binormal  $\vec{T} \times \vec{N} = \vec{B}$ , show that  $\vec{T} = \vec{N} \times \vec{B}$  and  $\vec{N} = \vec{B} \times \vec{T}$  and from  $\vec{T} = \vec{N} \times \vec{B}$  and  $\vec{N} = \vec{B} \times \vec{T}$  show that  $\vec{T} \times \vec{N} = \vec{B}$  Use properties of cross product.